The Cambridge Colour Test: Reliability of discrimination trivectors in colour space

**Background:** The reliable assessment of colour discrimination has become increasingly important as some ophthalmic diseases and systemic conditions manifest themselves via acquired impairments of colour vision. The Cambridge Colour Test (CCT) is a computerised procedure, developed using the basic principles of traditional pseudoisochromatic plates to evaluate colour function or discrimination.

**Aim:** The study investigated reliability of the CCT, with emphasis on the Trivector subtest, which measures thresholds along the three protan, deutan and tritan confusion lines to probe the sensitivity of the long, medium and short wavelength cones.

**Setting:** The study used a prospective observational and quantitative design and took place in a research and clinical environment within the Department of Optometry at the University of Johannesburg, South Africa. Participants were 20 young adults of both genders aged 19–24 years with normal colour vision.

**Methods:** Two measurements (test and retest) of the Trivector test were measured monocularly (right eye) for all participants to assess the reliability of repeated measurements. Reliability was assessed using coefficients of repeatability, coefficients of variation and Bland–Altman plots with limits of agreement (LoA).

**Results:** Outcomes for the Bland–Altman LoA showed good intra-individual agreement and coefficients of repeatability and reliability revealed generally high test–retest repeatability. Multivariate stereo-pair scatter plot comparisons of means and differences of test and retest measurements show that points cluster tightly within the same region in the three-dimensional colour space, and the centroids of the ellipsoids representing the mean differences are close to the origin at zero.

**Conclusion:** Although departure from normality and outlying values can have important influences, essentially the CCT provides very similar test and retest results for the Trivector test.

**Introduction**

The assessment of colour vision of an individual is an essential element of routine eye and vision examinations. Colour vision deficiencies are relatively common and defects of colour vision can be detected through a variety of tests. Colour vision and its deficiencies can be assessed qualitatively and quantitatively using tests that are grouped as arrangement tests, matching tests, vocational tests or pseudoisochromatic plates.

Specifically, a more sophisticated computerised procedure, the Cambridge Colour Test (CCT) (Cambridge Research Systems Ltd. [CRS], Rochester, United Kingdom), a diagnostic tool broadly used in both research and clinical settings, was developed using the basic principles of traditional pseudoisochromatic plates and modern technology of randomised luminance to evaluate chromatic sensitivity or discrimination based only on chromatic cues for detecting a target or pattern (a Landolt C in the case of the CCT). Unlike previous computerised colour vision tests, an advantage of this (CCT) computer-controlled test is the ability to adjust test difficulty depending on the patient’s performance, as well as random presentation of plates to reduce memorisation effects.

The CCT uses a computer version of pseudoisochromatic plates with two testing procedures, the Trivector subtest and the Ellipses subtest. The Ellipses test measures colour discrimination or sensitivity along 8, 12, 16 or 20 vectors or directions within a colour plane in the colour space (the Commission Internationale de l’Eclairage [the International Commission on Illumination] – CIE (1976) u’v’ space) to produce three discrimination or MacAdam ellipses that lie along the same
The CCT has been used in a variety of clinical studies and examples include the determination of colour discrimination losses in patients with ageing or possibly chronic diseases such as multiple sclerosis and for differential diagnostics of relative damage to chromatic pathways in conditions such as Parkinson’s disease. The CCT has also been adapted for use with animals such as squirrel monkeys, and the adapted version is said to be more reliable than other more conventional methods, because the stimulus parameters could be adjusted so that the animals were not able to use luminance differences to make correct discriminations.

This article concentrates on young adult observers with colour-normal vision to assess short-term test and retest repeatability and reliability of the CCT Trivector subtest. (Refer to the work by Hasrod for reliability and repeatability of the CCT Ellipses subtest.)

**Research objectives**

The primary aim of this study was to investigate in (colour-normal) human eyes the short-term test and retest reliability and reproducibility of results produced by the Trivector subtest of the CCT, using both univariate and multivariate statistical analyses. As such it may contribute or encourage greater use of the CCT in the future as a clinical or research tool to assess colour discrimination. Research on reliability in this study using multivariate statistics and methods was applied to CCT data, and some of these methods may possibly provide an easier way of analysing the trivariate (protn, deutan and tritan) vectors as unitary vectors (or points) in colour 3-space. This article demonstrates some of these methods.

**Methodology and design**

**Study design and setting**

The study used a prospective observational and quantitative design and took place in a research and clinical environment within the Department of Optometry at the University of Johannesburg, South Africa.

**Study population**

The study conformed to the tenets of the 2013 Declaration of Helsinki and was approved by the Higher Degrees and Ethics Committees of the university. The adult participants were predominantly of Caucasian (white) descent (60%) and 65% (or 13 of 20) were female. Mean age and standard deviation (s.d.) were 20.55 ± 1.43 years, the age range was from 19 to 24 years and the median age and quartile deviation (QD) were 20.00 ± 0.5 years. The mean auto-refraction of the 20 right eyes was -0.54–0.20 × 11. (Matrix methods were used to determine this mean.) Preliminary colour vision tests (the Farnsworth D15 test and the

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computerised Farnsworth-Munsell 100-hue test) were used to select participants with apparently normal colour vision. In addition, each participant’s right eye, to be tested using the CCT, underwent screening (biomicroscopy, ophthalmoscopy and refractive status; distant and proximal visual acuity) to estimate the appropriate habitual or spectacle compensation. Inclusion criteria were normal colour vision and a best compensated distance visual acuity of 6/9 or better. Exclusion criteria were factors that might influence colour vision adversely: history of congenital or acquired colour vision deficiencies, ocular disease, neurological or systemic diseases or use of medication known to affect colour vision.

Materials and data collection

Cambridge Research Systems Ltd. provided the necessary hardware and software for calibration and implementation procedures (ColorCAL colorimeter; calibration software and CRS/VSG 2/5 graphics card). Stimuli were displayed on a high resolution 22” monitor (HP CRT p1230) that was gamma-corrected. The CCT stimuli were computer-generated pseudoisochromatic images with each containing a Landolt C, as described, against a background comprised of circles of varying size, colour and luminance. A field or background of a single chromaticity or colour such as grey is used, but it is made up of smaller and larger discs that vary in terms of their luminances, which are randomised. The CCT test stimuli backgrounds are designed to eliminate luminance or contour cues; the figures (the test stimuli of Landolt letters) must be identified solely by their hues, and correct identification of the gaps or openings in the stimuli are used to confirm observer awareness of the stimuli themselves. Participants use a four-option response box to indicate openings.

A pilot study was conducted with two young adult participants to ascertain the duration of a session while employing both the Trivector and the Ellipses subtests. An experimental session for both tests took approximately 90 min and two sessions, for test and retest, were run either on the same day, separated by a short resting period, or on two consecutive days. However, most of the time was for the Ellipses test. Because of the time constraints and the actual testing time per test being between 20 min and 60 min, it was decided on the basis of the pilot study to measure only the 8-vector and 20-vector ellipses twice per participant in conjunction with the shorter Trivector test (which took approximately 3 min – 4 min per participant), which also would be done twice per participant. Here only data for the Trivector test will be included. Two measurements (test and retest) of the Trivector test were measured for all participants (n = 20) to assess the reliability of test and retest measurements.

Data analyses

Repeatability and reliability were assessed using hypothesis tests, intraclass correlation coefficients, coefficients of repeatability (CR), coefficients of variation (CV) and Bland–Altman plots with limits of agreement (LoA). The Bland–Altman plot may be used to assess the repeatability of a method by comparing repeated measurements using one single method on a series of subjects. The graph can also be used to check whether the variability or precision of a method is related to the size of the characteristic being measured. Furthermore, multivariate analysis by means of stereo-pair scatter plots was used to graphically demonstrate the short-term test and retest variation of results produced by the Trivector subtest.

Ethical considerations

The study conformed to the tenets of the 2013 Declaration of Helsinki and was approved (HDC01-24-2014 and AEC01-24-2014) by the Higher Degrees and Ethics Committees of the Faculty of Health Sciences, University of Johannesburg, South Africa.

Results

Hypothesis tests for normality in Table 1 formally test whether the population that the sample represents is likely to be normally distributed. The null hypothesis (H0) states that the sample (and population) is normally distributed, against the alternative hypothesis (H1) that it is not normally distributed. Shapiro–Wilks tests were utilised in conjunction with skewness and kurtosis coefficients in order to establish whether the Trivector test and retest measurements were well-modelled by normal distributions. The Shapiro–Wilks values (W) in Table 1 are between 0 and 1, with smaller values of W suggesting a rejection of normality and a value of 1 indicating normality of data. If the p-value is less than the chosen alpha level, namely 0.05, then the null hypothesis is rejected.

Thus, the proton vector’s test and retest samples and the deutan vector’s retest sample were drawn from normally distributed populations. However, the other three samples

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Note: All values in the first four columns (means, medians, IQR and s.d.) must be multiplied by 10° u/° units including the interquartile range and standard deviation. Skewness and kurtosis coefficients and Shapiro–Wilks results for the proton, deutan and tritan test and retest vectors for the Trivector test are also included. The sample consisted of 20 right eyes of young adults aged 19–24 years. IQR, interquartile range; s.d., standard deviation.
were not normally distributed. In conclusion, three samples (in Table 1) were normally distributed and three were not normally distributed. Therefore, non-parametric statistics were mainly applied here and box-and-whisker plots (Figure 2) were used to assess sample medians and the spread of data via interquartile ranges.

The skewness coefficients (γ) in Table 1 for the protan and deutan vectors were all close to zero and less than the standard errors of skewness (s.e.) value of ±1.095 (that is, $2\sqrt{\frac{6}{N}}$ or $2\sqrt{\frac{6}{20}}$), suggesting that with one exception (3.36), the data is not markedly skewed. The tritan vector’s retest skewness coefficient was 3.36 and, as with the normality plot, indicated that the data was positively right-skewed. The Pearson kurtosis index (κ) values (see Table 1) were slightly negative, suggesting minimal platykurtosis of data except for the tritan vector’s retest κ value of 13.17, indicating that this sample was markedly leptokurtic but an outlier had an effect on the normality of this sample.

The test and retest medians (Table 1 and Figure 2) for the vectors (P, D or T) were similar in value, suggesting little variation in test and retest medians. Looking at the spread of the data by means of their interquartile ranges (Table 1 and Figure 2), the values again were also mostly within a similar range, suggesting that relatively good consistency occurs between the test and retest responses. The very slightly larger range, suggesting that relatively good consistency occurs between the test and retest responses. The very slightly larger interquartile ranges and the ends of the whiskers are the minimum and maximum values. Each box-and-whisker plot is based on results for 20 right eyes of adults aged 19–24 years.

A multivariate analysis of the Trivector data was applied to further explore the samples. Multivariate data are used to better understand the associations or relations between multiple variables. Stereo-pair comets or trivariate discrimination vectors are used to provide a holistic and relatively simple graphical representation that joins test and retest vectors for the 20 right eyes concerned. The three axes of a 3-D (three-dimensional) graph or stereo-pair represents the protan (p), deutan (d) and tritan (t) vectors, respectively, for the eyes in the sample and each point in the stereo-pair scatter plot represents a unique combination of the protan, deutan and tritan components by the vector $e_i$ where

$$c_i = (p, d, t)$$ where $i = 1, 2, \ldots, \infty$. \[Eqn 1\]

The origin generally represents zero or (0 0 0). By plotting c on a set of three mutually orthogonal axes p, d and t, a three-dimensional scatter plot of a colour space is produced and the two halves of the scatter plot must be fused by allowing the eyes to diverge into an exo-position (fixation to an imaginary point behind the paper) to create the 3-D percept.

In Figure 3 a stereo-pair comet of test and retest results for each study participant can be illustrated graphically by means of joining a dot and a line segment with dots representing test vectors (e.g. $e_{\text{protan}} = (0.2 0.1 0.1)'$) of the colour response and the ends of lines representing corresponding retest vectors (e.g. $e_{\text{retest}} = (0.3 0.2 0.2)'$). Test values for the protan, deutan and tritan trivectors of a person can thus be represented via a single point and plotted within the 3-space. The same applies to the retest values for the same individual; then the comets (short line segments) can be used to link corresponding

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**Figure 2:** Box-and-whisker plots for the test (t) and retest (rt) Trivector measurements for the protan (P), deutan (D) and tritan (T) colour vectors.

**Note:** Small squares represent the medians of the respective vectors, the boxes are the interquartile ranges and the ends of the whiskers are the minimum and maximum values. Each box-and-whisker plot is based on results for 20 right eyes of adults aged 19–24 years. Units for the $y$-axis are CIE 1976 $\nu'\nu$ units.

CIE, International Commission on Illumination.

**FIGURE 2:** Box-and-whisker plots for the test (t) and retest (rt) Trivector measurements for the protan (P), deutan (D) and tritan (T) colour vectors.

Note: Each comet joins a test measurement (represented by a dot) to the end of the line (comet), being the retest measurement for a specific eye. Vectorial combinations of the protan ($p$), deutan ($d$) and tritan ($t$) vectors of the CCT Trivector test for 20 right eyes are, respectively, plotted along the three axes, with labels $p$, $d$ and $t$. Readers should allow their eyes to diverge to an imaginary point behind the figure when observing each of the halves of the stereo pairs. This will result in a third part appearing in the middle between the two halves of the stereo-pair and this central part will have a three-dimensional appearance.

**FIGURE 3:** Stereo pairs of a colour space with 20 comets joining the Cambridge Colour Test - Trivector test and retest measurements. The origin represents 0 $\nu'\nu$ units (or a chromatic Trivector $[p \ d \ t]'$ of [0 0 0]') and the axis lengths are 0.01 $\nu'\nu$ units.
test and retest trivectors for the eye concerned, and the lengths of the comets are a qualitative (and quantitative) measure of the similarity or equality of test and retest trivectors for that individual. Variations between test and retest results for different eyes then can be easily compared and, depending on the scale, shorter distances between two points show little variation in test and retest measurements. Points or comets that cluster within the same region will also indicate that measurements are similar in value.27

In Figure 3 there are 20 comets (one for each participant) and it can be seen that most of the test and retest measurements appear to be similar, with perhaps three or four exceptions, and particularly the comet and point indicated with the arrows where test and retest measurements are dissimilar for the participant concerned. This comet roughly parallels the tritan axis, suggesting that test and retest measurements for the tritan coordinates were more variable. Excluding this comet, all other comets are clustered closely together in the colour 3-space.

Figure 4 represents the test and retest stereo-pair scatter plots and 95% surfaces of constant probability density (approximately 95% of sample measurements are expected to be found within each ellipsoid).27 Test and retest measurements are indicated by black or magenta points, respectively, and most measurements for the test and retest samples cluster about the means of the samples concerned. When viewing the scatter plots in three-dimensional space, both the test and retest measurements seem to cluster within the same region, indicating similarity, but both samples vary more with respect to the axis for the tritan coordinates, with the principal diameters of the ellipsoids almost paralleling this axis. The larger distribution ellipsoid for the magenta suggests greater variation of measurements compared to test measurements. However, an outlying value (the magenta dot above the magenta ellipsoid) is important and its removal would result in the magenta ellipsoid becoming smaller and more similar to the black (test) one. In Table 2 some basic statistics for the two samples are provided.

Variance and covariances indicate the variability and linear relationships, respectively, between the test and retest trivectors (protan, deutan and tritan) in the 3-space. If no variation exists, then all six entries will be zero.26 Overall variances were found to be slightly greater for the Trivector retest measurements (Tri-rt) but an outlying value was important. Also greater test and retest variation was found for the tritan coordinates (t). All covariances were close to zero; thus minimal or no linear relationships between paired variances exist, and variance for a specific vector along a confusion axis, for example, protan variance, is not linearly related to the variance along the confusion axes of either of the other two vectors (deutan or tritan).

Reliability statistics

Bland–Altman plots in Figure 5 and corresponding statistics (see Table 3) are used to investigate repeatability of the Trivector test by comparing test and retest measurements for the trivectors along three confusion lines for 20 right eyes and plotting their differences against their means.

The horizontal solid red line (Figure 5a) in each plot indicates the mean difference (Δ) or estimated bias of the 20 paired measurements, with the distance from zero (no difference) providing an estimate of the average difference between the two methods. Theoretically, if both samples of measurements were identical and free from error, the mean difference would be zero and the further away the mean difference is from zero, the larger the magnitude of the bias; in this instance, as the test values were subtracted from the retest values, a positive mean difference would indicate that, on average, the retest values are slightly larger. The 95% LoA are indicated in Figure 5a using dashed lines, and the lines (solid or dashed) also include 95% confidence intervals (the shaded regions about the upper and lower LoA). These LoA were calculated using 1.96 times the standard deviation of the differences between the two samples (d = d - t) where d = retest and t = test) under the assumption of normally distributed differences.

Mean differences (Δ) (see Figure 5 and Table 3) for the trivectors in the Bland–Altman plots are very close to zero, suggesting that on average, for these 20 right eyes, not much difference occurs between the test and retest results produced by the Trivector test. The means and differences are not correlated (r = 0.42, p = 0.071).

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<td>Tri-rt</td>
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Note: Variances of protan (S_p), deutan (S_d) and tritan (S_t) vectors for 20 right eyes of adults aged 19–24 years are represented. S_p represents the variance of the protan and deutan vectors, S_d represents the covariance of the tritan and protan vectors and S_t represents the covariance of the tritan and deutan vectors. The units are u'v' = 10^-4 for the means and [u'v']^2 = 10^-4 for variances and covariances.
When looking at the upper and lower LoA (Figure 5), it can be seen that the interval is slightly larger for the tritan vectors and this suggests the tritan vectors have slightly more variability in results yielded by the 20 subjects. Further calculations indicated that the tritan differences (between test and retest) were not normally distributed; therefore an additional Bland–Altman plot using medians (±95% LoA) was provided in Figure 5d.

The median difference (solid line) (Figure 5d and Table 3) was –0.0007 $u'v'$ units and the 95% confidence interval (dashed lines) was (–0.0026; 0.0004) $u'v'$ units. The first number in the brackets is the lower limit and the second the upper limit; note the asymmetry in the interval relative to the solid line (median difference). The 95% confidence interval length for the LoA changed from 0.02 to 0.003 $u'v'$ in Figure 5c and d, respectively.

Because the International Organisation for Standardisation recommends expressing repeatability in terms of standard deviations, the CR can be calculated as 1.96 (or 2) times the mean difference.
standard deviation of the differences between the two samples ($d_2$ and $d_1$ where $d_2 =$ retest and $d_1 =$ test):\[ \text{CR} = 1.96 \times \sqrt{\frac{\sum(d_2 - d_1)^2}{n-1}}. \] [Eqn 2]

This coefficient can also be read from a corresponding Bland–Altman plot by subtracting the mean difference ($\bar{d}$) from the upper 95% LoA. If the differences between two samples are all zero, then CR = 0, and the greater the value for CR the less similar are the test and retest measurements.\[ \text{Table 3 has CR} = 0.01 \text{ for all samples, and this indicates excellent repeatability between test and retest samples.} \]

The CV represents the ratio of the standard deviation ($\sigma$) of the population to the population mean ($\mu$), and it is a useful statistic for comparing the degree of variation from one data series to another, even if the means are drastically different from each other. The CV is defined as follows:\[ CV = \frac{\sigma}{\mu}. \] [Eqn 3]

Thus CV shows the extent of variability in relation to the mean of the sample or population. If the sample parameters ($\sigma$ and $\mu$) are unknown, then CV can be estimated as a ratio of the sample standard deviation divided by the sample mean.\[ \text{If CV} < 1, \text{ there is low variance between samples, for example test and retest samples, and high variance occurs when CV} > 1. \]

Both the CR and CV in Table 3 suggest that the CCT Trivector test produces repeatable results with low variation occurring within the test and retest samples.

The stereo-pair in Figure 6 mimics an ordinary Bland–Altman plot but with a multivariate approach instead in order to assess repeatability.\[ \text{The means of the test and retest} \]

ellipsoids, the greater the variation in the differences and/or means. The greater the differences and its ellipsoid, the weaker the repeatability between test and retest measurements (CCT trivectors in this case).\[ \text{Although the ellipsoids in Figure 6 look relatively large, the axis lengths are only 0.01 } \mu \text{ units. If, for example, axes of 1 } \mu \text{ units were used instead, the ellipsoids would be seen to be very small. (Thus the scale applied needs to be taken into careful consideration when interpreting the meaning of the results.)} \]

When analysing the stereo-pair scatter plots for the means of the samples versus their differences (see Figure 6 and Table 4), the Trivector tests for the 20 right eyes produce test and retest results that are consistent and repeatable. The differences in magenta can be seen as being more variable than the means in cyan. That is, the magenta points are more widely spread and their 95% distribution ellipsoid is larger than for the cyan points and their corresponding ellipsoid (an outlier was important here). However, the ellipsoids for both the differences and the means are more variable with respect to the tritan axis (and tritan coordinate vectors). Variances suggest higher variability with the tritan vectors. Covariances, although larger when the tritan vector is involved, are close to zero, indicating no linear relationships between the various coordinate vectors.
Hypothesis tests

The Wilcoxon test is a non-parametric equivalent of the parametric paired t-test and is used to test for a difference in the mean (or median) of paired observations – before and after measurements with the same units and in Table 5, results represent the test and retest measurements for the Trivector tests for 20 right eyes. With this test, if the p-value is less than 0.05, we can reject the null hypothesis and the sample being compared, for example, test and retest measurements significantly differ. From Table 5, we are confident in saying that test and retest measurements produced by the Trivector test are repeatable and reliable as the p-values of these tests are greater than the significance level of 0.05.

When hypothesis tests for equality of means or equality of variances and covariances are applied to the test and retest Trivector data (Figure 4 and Table 5), the null hypothesis is accepted as equal variances, covariances and means are present, therefore implying that the Trivector test produces test and retest results for these 20 right eyes that are consistent and repeatable.

Discussion

Three samples (in Table 1) for the Trivector results were normally distributed and three were not normally distributed. A possible reason for the results for some of these samples (such as for the tritan vector being not normally distributed) could be the presence of outlying values in the test and/or retest measurements for the sample of 20 right eyes. Fatigue or lack of concentration perhaps could have influenced the tritan retest measurement as this participant (that is, the outlier) showed no tritan deficiency with the preliminary colour vision tests; therefore, a removal of this possible outlier from the sample would perhaps influence the distribution in terms of normality. The sample size (n = 20) was also relatively small and this might also have been a contributing factor.

The tritan vector medians, interquartile ranges and standard deviations, while very similar (for test and retest samples), were larger than those for the protan and deutan vector medians, suggesting that the participants were probably less sensitive along the tritan confusion line and one or more outlying values were also important.

Using Bland–Altman plots and LoA (Figure 5 and Table 3), mean differences and the 95% LoA are small for the protan, deutan and tritan measurements, suggesting that differences and mean differences between test and retest measurements are small, and thus test and retest results for the Trivector test are in good agreement. Coefficients of repeatability and variation values and Bland–Altman LoA are more decisive for conclusions on repeatability and reliability, and these measures indicate good agreement between test and retest for the Trivector test as values are close to zero.

Table 6 compares the means, standard deviations, medians and QDs (QD = IQR) for results for the Trivector test from this article (in Johannesburg) to a study from Liverpool for 40 subjects in the 20–29-year age group (mean ages were 22.6 ± 2.8 years) and combined data from a study in Brazil for 75 subjects aged 18–30 years, that is, the São Paulo group of 45 subjects with mean ages of 22.5 ± 2.7 years and the Belem group of 30 subjects with mean ages of 21.8 ± 2.9 years.

From Table 6, results for the Trivector test show that means were similar for the groups in Liverpool and Brazil, although generally the means were lower in the Liverpool sample. Parameters states that a factor that may result in some differences in statistical data could be the use of the CCT software, as the Belem group ran the CCT using a self-built system (IBM RISC 6000) and self-developed software, and the São Paulo and Liverpool groups employed the CCT commercial version (v2.0; VSG 5 card; CRS). In this study, Trivector means and standard deviations mostly were slightly larger (however, quantities in Table 6 are quite small and should be multiplied by 10), and possible reasons for this could be influence of outlying values and the smaller sample size used in comparison to the other studies.

Medians are less influenced by outliers, and, if one compares the results in this study to the medians (in Liverpool) and means (in Liverpool and Brazil) of the other studies, the medians for the proton, deutan and tritan vectors are still larger, suggesting that outliers and/or sample size may have an influence on the inflation of results. In terms of standard deviations and QDs, results in this article are similar to the other studies for the deutan vectors but slightly larger for the proton vectors and particularly for the tritan vectors. Again, differences in sample sizes across the studies and the influence of outlying values are relevant issues. It can be seen, however, that across the studies, the tritan vector generally had larger colour values, suggesting that subjects are less sensitive along the tritan confusion line than along the proton or deutan confusion lines.
test and retest trivariate data can be explored in a 3-space in terms of means and differences. This three-dimensional graphical approach has not previously been applied to Trivector results but has recently been used with other data such as contrast visual acuities.30 However, comparisons of means and differences of test and retest measurements herein showed that the majority of the Trivector test and retest means cluster in front of and vary mainly in a direction almost parallel to the tritan axis, indicating greater variability for the tritan vectors. The differences between test and retest measurements mostly cluster near the origin (or zero difference), and the centroid of the ellipsoid (or mean difference, \(\bar{X}_d\)) is also close to the origin at zero, indicating good repeatability of data. Variances (see Table 3) confirm that the data for the tritan vectors for the sample of 20 right eyes are the most variable of the three vectors, and covariances are close to zero, indicating a lack of linear relationship between variances for any of the three colour vectors concerned. The volumes of the Trivector means and differences ellipsoids are also small, indicating consistency and good agreement; however, the differences can be seen as being more variable than the means.

Also, importantly, despite the relatively small sample size and the possibility of outliers, univariate and multivariate hypothesis tests found that the test and retest samples for all three vectors were not significantly different in terms of their means and standard deviations. Thus, Trivector results were reliable, and this is an important result in terms of supporting future clinical and research applications.

## Conclusion

Through comprehensive analyses of Trivector results produced by the CCT on healthy human eyes with normal trichromatic vision, reliability and repeatability of the test and retest measurements were established. Although departure from normality and outlying values can have important influences, essentially, the CCT provides very similar test and retest results for the Trivector test. The Trivector test thus can be used with confidence by researchers or clinicians, as it provides reliable results in repeated measures.

### Acknowledgements

The authors declare that they have no financial or personal relationships that may have inappropriately influenced them in writing this article.

### Authors’ contributions

N.H. collected the data and wrote the manuscript as part of her master’s dissertation, with supervision by A.R. Review of the initial draft, supervision and approval of the manuscript were performed by A.R.

### References


### Table 6: Comparisons of means and standard deviations for the Cambridge Colour Test Trivector test between studies (Brazil and Liverpool) and this study; medians and quartile deviation are included for Johannesburg and Liverpool

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<tr>
<td>Averaged (t and rt)</td>
<td>-</td>
<td>-</td>
<td>58.9 (16.8)</td>
</tr>
<tr>
<td>Medians</td>
<td>40.5</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>QD</td>
<td>6.5</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Medians (t)</td>
<td>-</td>
<td>-</td>
<td>52.0</td>
</tr>
<tr>
<td>QD (t)</td>
<td>-</td>
<td>-</td>
<td>8.8</td>
</tr>
<tr>
<td>Medians (rt)</td>
<td>-</td>
<td>-</td>
<td>62.5</td>
</tr>
<tr>
<td>QD (rt)</td>
<td>-</td>
<td>-</td>
<td>13.8</td>
</tr>
<tr>
<td>Averaged (t and rt)</td>
<td>-</td>
<td>-</td>
<td>57.3 (11.3)</td>
</tr>
</tbody>
</table>

Note: Each statistic should be multiplied by 10^{-4} \(u'v'\) units. For example, for the red (protan) vectors in Liverpool and Johannesburg, the means and standard deviations are 0.00423 ± 0.00095 \(u'v'\) units and 0.00554 ± 0.00147 \(u'v'\) units, respectively.

| t, test; rt, retest; s.d., standard deviation; QD, quartile deviation. |


37. Sukha AY. Inter- and intra-subject variation of contrast visual acuities. DPhil thesis, Johannesburg, South Africa: Department of Optometry, Faculty of Health Sciences, University of Johannesburg; 2015.